



Designation: E2070 – 13 (Reapproved 2018)

Standard Test Methods for Kinetic Parameters by Differential Scanning Calorimetry Using Isothermal Methods¹

This standard is issued under the fixed designation E2070; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ϵ) indicates an editorial change since the last revision or reapproval.

1. Scope

1.1 Test Methods A, B, and C determine kinetic parameters for activation energy, pre-exponential factor and reaction order using differential scanning calorimetry from a series of isothermal experiments over a small (≈ 10 K) temperature range. Test Method A is applicable to low n th order reactions. Test Methods B and C are applicable to accelerating reactions such as thermoset curing or pyrotechnic reactions and crystallization transformations in the temperature range from 300 to 900 K (nominally 30 to 630°C). These test methods are applicable only to these types of exothermic reactions when the thermal curves do not exhibit shoulders, double peaks, discontinuities or shifts in baseline.

1.2 Test Methods D and E also determines the activation energy of a set of time-to-event and isothermal temperature data generated by this or other procedures

1.3 The values stated in SI units are to be regarded as standard. No other units of measurement are included in this standard.

1.4 These test methods are similar but not equivalent to ISO DIS 11357, Part 5, and provides more information than the ISO standard.

1.5 *This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety, health, and environmental practices and determine the applicability of regulatory limitations prior to use.* Specific precautionary statements are given in Section 8.

1.6 *This international standard was developed in accordance with internationally recognized principles on standardization established in the Decision on Principles for the Development of International Standards, Guides and Recommendations issued by the World Trade Organization Technical Barriers to Trade (TBT) Committee.*

2. Referenced Documents

2.1 ASTM Standards:²

- D3350 Specification for Polyethylene Plastics Pipe and Fittings Materials
- D3895 Test Method for Oxidative-Induction Time of Polyolefins by Differential Scanning Calorimetry
- D4565 Test Methods for Physical and Environmental Performance Properties of Insulations and Jackets for Telecommunications Wire and Cable
- D5483 Test Method for Oxidation Induction Time of Lubricating Greases by Pressure Differential Scanning Calorimetry
- D6186 Test Method for Oxidation Induction Time of Lubricating Oils by Pressure Differential Scanning Calorimetry (PDSC)
- E473 Terminology Relating to Thermal Analysis and Rheology
- E537 Test Method for The Thermal Stability of Chemicals by Differential Scanning Calorimetry
- E698 Test Method for Kinetic Parameters for Thermally Unstable Materials Using Differential Scanning Calorimetry and the Flynn/Wall/Ozawa Method
- E967 Test Method for Temperature Calibration of Differential Scanning Calorimeters and Differential Thermal Analyzers
- E968 Practice for Heat Flow Calibration of Differential Scanning Calorimeters
- E1142 Terminology Relating to Thermophysical Properties
- E1445 Terminology Relating to Hazard Potential of Chemicals
- E1858 Test Methods for Determining Oxidation Induction Time of Hydrocarbons by Differential Scanning Calorimetry
- E1860 Test Method for Elapsed Time Calibration of Thermal Analyzers
- E1970 Practice for Statistical Treatment of Thermoanalytical Data

¹ These test methods are under the jurisdiction of ASTM Committee E37 on Thermal Measurements and is the direct responsibility of Subcommittee E37.01 on Calorimetry and Mass Loss.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

E2041 Test Method for Estimating Kinetic Parameters by Differential Scanning Calorimeter Using the Borchardt and Daniels Method

E2046 Test Method for Reaction Induction Time by Thermal Analysis

2.2 *ISO Standard*.³

ISO DIS 11357 Part 5: Determination of Temperature and/or Time of Reaction and Reaction Kinetics

3. Terminology

3.1 Specific technical terms used in these test methods are defined in Terminologies **E473**, **E1142**, and **E1445**, including the terms *calorimeter*, *Celsius*, *crystallization*, *differential scanning calorimetry*, *general rate law*, *isothermal*, *peak*, and *reaction*.

4. Summary of Test Method

4.1 A test specimen is held at a constant temperature in a differential scanning calorimeter throughout an exothermic reaction. The rate of heat evolution, developed by the reaction, is proportional to the rate of reaction. Integration of the heat flow as a function of time yields the total heat of reaction.

4.2 An accelerating (Sestak-Berggren or Avrami models), n th order data, or model free treatment^{4,5,6} is used to derive the kinetic parameters of activation energy, pre-exponential factor and reaction order from the heat flow and total heat of reaction information obtained in 4.1. (See Basis for Methodology, Section 5.)

5. Basis of Methodology

5.1 Reactions of practical consideration are exothermic in nature; that is, they give off heat as the reaction progresses. Furthermore, the rate of heat evolution is proportional to the rate of the reaction. Differential scanning calorimetry measures heat flow as a dependent experimental parameter as a function of time under isothermal experimental conditions. DSC is useful for the measurement of the total heat of a reaction and the rate of the reaction as a function of time and temperature.

5.2 Reactions may be modeled with a number of suitable equations of the form of:

$$da/dt = k(T) f(\alpha) \quad (1)$$

where:

da/dt = reaction rate (s^{-1}),

α = fraction reacted (dimensionless),

$k(T)$ = specific rate constant at temperature T (s^{-1}),

$f(\alpha)$ = conversion function. Commonly used functions include:

$$f_1(\alpha) = (1 - \alpha)^n \quad (2)$$

$$f_2(\alpha) = \alpha^m (1 - \alpha)^n \quad (3)$$

$$f_3(\alpha) = p(1 - \alpha)[-1/n(1 - \alpha)]^{(p-1)/p} \quad (4)$$

³ Available from American National Standards Institute (ANSI), 25 W. 43rd St., 4th Floor, New York, NY 10036, <http://www.ansi.org>.

⁴ Sbirrazzuoli, N., Brunel, D., and Elegant, L., *Journal of Thermal Analysis*, Vol 38, 1992, pp. 1509–1524.

⁵ Sestak, J., and Berggren, G., *Thermochemica Acta*, Vol 3, 1971, p. 1.

⁶ Gorbachiev, V.M., *Journal of Thermal Analysis*, Vol 18, 1980, pp. 193–197.

where:

n , m , and p = partial reaction order terms.

NOTE 1—There are a large number of conversion function expressions for $f(\alpha)$.⁴ Those described here are the most common but are not the only functions suitable for these test methods. Eq 1 is known as the general rate equation while Eq 3 is the accelerating (or Sestak-Berggren) equation.^{5,6}

Eq 4 is the accelerating Avrami equation. Eq 2 is used for n th order reactions while Eq 3 or Eq 4 are used for accelerating reaction, such as thermoset cure and crystallization transformations.

5.3 For a reaction conducted at temperature (T), the accelerating rate Eq 3 and the rate equation Eq 1 may be cast in their logarithmic form.

$$da/dt = k(T) \alpha^m (1 - \alpha)^n \quad (5)$$

$$\ln[da/dt] = \ln[k(T)] + m \ln[\alpha] + n \ln[1 - \alpha] \quad (6)$$

This equation has the form $z = a + bx + cy$ and may be solved using multiple linear regression analysis where $x = \ln[\alpha]$, $y = \ln[1 - \alpha]$, $z = \ln[da/dt]$, $a = \ln[k(T)]$, $b = m$ and $c = n$.

NOTE 2—The rate equation (Eq 3) reduces to the simpler general rate equation (Eq 2) when the value of reaction order parameter m equals zero thereby reducing the number of kinetic parameters to be determined.

5.4 For reactions conducted at temperature (T), the accelerating rate equation of Eq 4 may be cast as:

$$\ln[-\ln(1 - \alpha)] = p \ln[k(T)] + p \ln[t] \quad (7)$$

This equation has the form of $y = mx + b$ and may be solved by linear regression where $x = \ln[t]$, $y = \ln[-\ln(1 - \alpha)]$, with $p = m$, $b = p \ln[k(T)]$, and $t = \text{time}$.

5.5 The Arrhenius equation describes how the reaction rate changes as a function of temperature:

$$k(T) = Z e^{-E/RT} \quad (8)$$

where:

Z = pre-exponential factor (s^{-1}),

E = activation energy ($J \text{ mol}^{-1}$),

T = absolute temperature (K),

R = gas constant ($8.314 \text{ J mol}^{-1} \text{ K}^{-1}$), and

e = natural logarithm base = 2.7182818.

5.6 Eq 8 cast in its logarithmic form is:

$$\ln[k(T)] = \ln[Z] - E/RT \quad (9)$$

Eq 9 has the form of a straight line, $y = mx + b$, where a plot of the logarithm of the reaction rate constant ($\ln[k(T)]$) versus the reciprocal of absolute temperature ($1/T$) is linear with the slope equal to $-E/R$ and an intercept equal to $\ln[Z]$.

5.7 As an alternative to Eq 6 and Eq 7, the rate and Arrhenius equations combined and cast in logarithmic form is:

$$\ln[da/dt] = \ln[Z] - E/RT + m \ln[\alpha] + n \ln[1 - \alpha] \quad (10)$$

Eq 10 has the form, $z = a + bx + cy + dw$, and may be solved using multiple linear regression analysis.

where:

z = $\ln[da/dt]$

a = $\ln[Z]$

b = $-E/R$

x = $1/T$

c = m

y = $\ln[1 - \alpha]$

$d = n$, and
 $w = \ln[1 - \alpha]$.

5.8 If activation energy values only are of interest, Eq 11 may be solved under conditions of constant conversion to yield:

$$\ln[\Delta t] = E/RT + b \quad (11)$$

where:

Δt = lapsed time (s), at constant conversion and at isothermal temperature, T , and

b = constant.

Eq 11 has the form of a straight line, $y = mx + b$, where a plot of the logarithm of the lapsed time under a series of differing isothermal conditions versus the reciprocal of absolute temperature ($1/T$) is linear with a slope equal to E/R .

5.9 If activation energy values only are of interest, Eq 11 may be solved under conditions of constant conversion and the equality $da/dt = dH/dt / (H)$ to yield:

$$\ln[dH/dt] = -E/RT + b = m/T + b \quad (12)$$

where:

H = total heat of reaction (mJ),

dH/dt = instantaneous heat flow (mW),

b = constant, and

m = slope (K)

Eq 12 has the form of a straight line $y = mx + b$, where a plot of the logarithm of the heat flow ($\ln[dH/dt]$) at the peak of the exotherm under a series of differing isothermal temperature conditions versus the reciprocal of the absolute temperature ($1/T$) is linear with a slope equal to E/R .

5.10 A series of isothermal experiments by Test Method A, B, and C described in Section 11 at four or more temperatures, determines the kinetic parameters of activation energy, pre-exponential factor and reaction order. Alternatively, the time to a condition of constant conversion for a series of experiments at four or more temperatures obtained by this or alternative Test Method D, described in Section 12, may be used to determine activation energy only.

5.11 A series of not less than four isothermal DSC experiments, covering a temperature range of approximately 10 K and a time less than 100 min (such as those shown in Fig. 1) provides values for da/dt , α , $(1 - \alpha)$ and T to solve Eq 6, Eq 7, Eq 9, and Eq 10.

5.12 A series of not less than four isothermal DSC experiments covering a temperature range of approximately 10 K and a time less than 100 min provides dH/dt and T to solve Eq 12

5.13 A variety of time-to-event experiments such as oxidation induction time methods (Specification D3350 and Test Methods D3895, D4565, D5483, D6186, and E1858) and reaction induction time methods (Test Method E2046) provide values for Δt and T to solve equation Eq 11.

6. Significance and Use

6.1 These test methods are useful for research and development, quality assurance, regulatory compliance, and specification acceptance purposes.

6.2 The determination of the order of a chemical reaction or transformation at specific temperatures or time conditions is beyond the scope of these test methods.

6.3 The activation energy results obtained by these test methods may be compared with those obtained from Test Method E698 for n th order and accelerating reactions. Activation energy, pre-exponential factor, and reaction order results by these test methods may be compared to those for Test Method E2041 for n th order reactions.

7. Interferences

7.1 The approach is applicable only to exothermic reactions.

NOTE 3—Endothermic reactions are controlled by the rate of the heat transfer of the apparatus and not by the kinetics of the reaction and may not be evaluated by these test methods.

7.2 These test methods are intended for a reaction mechanism that does not change during the transition. These test methods assume a single reaction mechanism when the shape of the thermal curve is smooth (as in Fig. 2 and Fig. 3) and does not exhibit shoulders, multiple peaks, or discontinuation steps.

7.3 Test method precision is enhanced with the selection of the appropriate conversion function [$f(\alpha)$] that minimizes the number of experimental parameters determined. The shape of the thermal curve, as described in Section 11, may confirm the selection of the n th order or accelerating models.

7.4 Typical n th order reactions include those in which all but one of the participating species are in excess.

7.5 Typical accelerating reactions include thermoset cure, crystallization and pyrotechnic reactions.

7.6 For n th order kinetic reactions, these test methods anticipate that the value of n is small, non-zero integers, such as 1 or 2. These test methods should be used carefully when values of n are greater than 2 or are not a simple fraction, such as $1/2 = 0.5$.

7.7 Accelerating kinetic reactions anticipate that m and n are fractions between 0 and 2 and that their sum ($m + n$) is less than 3.

7.8 Accelerating kinetic reactions anticipate that p is an integer often with a value of ≤ 4 .

7.9 Since these test methods use milligram quantities, it is essential that the test specimens are homogeneous and representative of the larger samples from which they are taken.

7.10 Test specimens may release toxic and corrosive effluents that may be harmful to personnel or apparatus. Operation with a venting or exhaust system is recommended.